

# STATISTICS

|                    |  |   |
|--------------------|--|---|
| Mean               | $\bar{x} = \frac{\sum x}{n}$   |   |
| Median             | If $n$ is odd, then<br>$M = \left(\frac{n+1}{2}\right)^{\text{th}} \text{ term}$ | If $n$ is even, then<br>$M = \frac{\left(\frac{n}{2}\right)^{\text{th}} \text{ term} + \left(\frac{n+1}{2}\right)^{\text{th}} \text{ term}}{2}$ |
| Mode               | The value which occurs most frequently   |   |
| Variance           | $\sigma^2 = \frac{\sum (x - \bar{x})^2}{n}$                                      |   |
| Standard Deviation | $S = \sigma = \sqrt{\frac{\sum (x - \bar{x})^2}{n}}$                             |   |

$x$  = observations given  
 $n$  = Total no. of observations  
 $\bar{x}$  = Mean

✓ Range = Maximum value - Minimum value

✓ Mean Deviation M.D.(a) =  $\frac{\text{Sum of absolute values of deviations from 'a'}}{\text{No. of observations}}$

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

✓ Mean deviation for ungrouped data Let  $n$  observations be  $x_1, x_2, x_3, \dots, x_n$ .

$$\text{M.D.}(\bar{x}) = \frac{1}{n} \sum_{i=1}^n |x_i - \bar{x}| \quad \& \quad \text{M.D.}(M) = \frac{1}{n} \sum_{i=1}^n |x_i - M|$$

$\bar{x}$  = Mean  
 $M$  = Median

✓ Mean deviation for grouped data

$$(\bar{x}) = \frac{1}{N} \sum_{i=1}^n f_i$$

$$\text{M.D.}(\bar{x}) = \frac{1}{N} \sum_{i=1}^n f_i |x_i - \bar{x}|$$

$$\text{M.D.}(M) = \frac{1}{N} \sum_{i=1}^n f_i |x_i - M|$$

, where  $N = \sum_{i=1}^n f_i$

✓ Shortcut method for calculating mean deviation about mean

$$\bar{x} = a + \frac{\sum_{i=1}^n f_i d_i}{N} \times h$$

$$\text{Median} = l + \frac{\frac{N}{2} - C}{f} \times h$$

assumed mean

common factor

✓ Variance and standard deviation

✓ Coefficient of variation (C.V.)

$$\frac{\sigma}{\bar{x}} \times 100, \quad \bar{x} \neq 0$$

$$\sigma^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$$

$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2}$$

Variance ( $\sigma^2$ )  
Standard deviation ( $\sigma$ )

✓ Variance and standard deviation of a discrete frequency distribution

$$\sigma^2 = \frac{1}{N} \sum_{i=1}^n f_i (x_i - \bar{x})^2$$

$$\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^n f_i (x_i - \bar{x})^2}$$

✓ Variance and standard deviation of a continuous frequency distribution

$$\sigma^2 = \frac{1}{N} \sum_{i=1}^n f_i (x_i - \bar{x})^2$$

$$\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^n f_i (x_i - \bar{x})^2}$$

$$\text{OR } \sigma = \sqrt{\frac{1}{N} \sum_{i=1}^n f_i x_i^2 - (\frac{1}{N} \sum_{i=1}^n f_i x_i)^2}$$

✓ Shortcut method to find variance and standard deviation

$$\sigma^2 = \frac{h^2}{N^2} \left[ N \sum_{i=1}^n f_i y_i^2 - (\sum_{i=1}^n f_i y_i)^2 \right]$$

$$\sigma = \frac{h}{N} \sqrt{N \sum_{i=1}^n f_i y_i^2 - (\sum_{i=1}^n f_i y_i)^2}$$

where  $y_i = \frac{x_i - A}{h}$

